# Unit 3 The Relational Model

# Outline

- **3.1** Introduction
- □ 3.2 Relational Data Structure
- □ 3.3 Relational Integrity Rules
- □ 3.4 Relational Algebra
- □ 3.5 Relational Calculus

# **3.1 Introduction**

# Relational Model [Codd '70]



- representing data: by means of tables
- manipulating that representation: by select, join, ...

# Relational Model (cont.)

- Concerned with three aspects of data:
  - 1. Data structure: tables
  - 2. Data integrity: primary key rule, foreign key rule
  - 3. <u>Data manipulation:</u> (Relational Operators):
    - Relational Algebra (See Section 3.4)
    - Relational Calculus (See <u>Section 3.5</u>)
- Basic idea: relationship expressed in data values, not in link structure.

<e.g.></e.g.>	<u>Entity</u> Mark	<b>Rela</b> Wo	<b>ationship</b> rks_in	<u>En</u> Mat	<u>tity</u> h_Dept
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# Terminologies

- Relation : so far corresponds to a *table*.
- Tuple : a *row* of such a table.
- Attribute : a *column* of such a table.
- Cardinality : **number of tuples.**
- Degree : number of attributes.
- Primary key : an attribute or attribute combination that uniquely identify a tuple.
- Domain : a pool of legal values.



# **3.2 Relational Data Structure**

# Domain

- Scalar: the smallest semantic unit of data, atomic, nondecomposable.
- **Domain**: a set of scalar values with the same type.
- Domain-Constrained Comparisons: two attributes defined on the same domain, then comparisons and hence joins, union, etc. will make sense.



• A system that supports domain will prevent users from making <u>silly</u> mistakes.

### Domain (cont.)

• Domain should be specified as part of the database definition.

<e.g.></e.g.>			
CREATE	DOMAIN	S#	CHAR(5)
CREATE	DOMAIN	NAME	CHAR(20)
CREATE	DOMAIN	STATUS	SMALLINT;
CREATE	DOMAIN	CITY	CHAR(15)
CREATE	DOMAIN	P#	CHAR(6)
CREATE	TABLE S		
	(S# <u>D</u> O SNAME DO	OMAIN (S#) No OMAIN (NAME)	ot Null
	•		
CDEATE	TARIE D		
CREATE	(P#	DOMAIN (P	#) Not Null
	PNAME	DOMAIN (N	AME)
		Dominiv(iv	· · · · · · · · · · · · · · · · · · ·
	•		
CREATE	TABLE SP		
	(S# DOMA	AIN (S#) Not Nu	ıll,
	P# DOMA	AIN (P#) Not Nu	11,

• **Composite domains**: a combination of simple domains.

< e.g. > DATE = MONTH(1..12) + DAY(1..31) + YEAR(0..9999)

CREATE	DOMAIN	MONTH	CHAR(2);
CREATE	DOMAIN	DAY	CHAR(2);
CREATE	DOMAIN	YEAR	CHAR(4);
CREATE	DOMAIN	DATE	
	(MONTH	DOMAIN	(MONTH),
	DAY	DOMAIN	(DAY),
	YEAR	DOMAIN	(YEAR));

# Relations

Definition : A relation on domains D<sub>1</sub>, D<sub>2</sub>, ..., D<sub>n</sub> (not necessarily all distinct) consists of a <u>heading</u> and a <u>body</u>.

heading body

S#	SNAME	STATUS	CITY
<b>S</b> 1	Smith	20	London
S4	Clark	20	London

- *Heading* : a <u>fixed set</u> of attributes  $A_1, ..., A_n$  such that  $A_j$  underlying domain  $D_j$  (j=1...n).
- *Body:* a <u>time-varying</u> set of tuples.
- *Tuple:* a set of attribute-value pairs. {A<sub>1</sub>:Vi<sub>1</sub>, A<sub>2</sub>:Vi<sub>2</sub>,..., A<sub>n</sub>:Vi<sub>n</sub>}, where I = 1...m or { $t_1, t_2, t_3, ..., t_m$ }

# **Properties of Relations**

- There are no duplicate tuples: since **relation** is a **mathematical set.** 
  - *Corollary* : the primary key always exists.

(at least the combination of all attributes of the relation has the uniqueness property.)

- Tuples are unordered.
- Attributes are unordered.
- All attribute values are <u>atomic</u>.
  - i.e. There is only one value, not a list of values at every row-and-column position within the table.
  - i.e. Relations do not contain repeating groups.
  - i.e. Relations are *normalized*.

### **Properties of Relations** (cont.)

Normalization



### **Properties of Relations** (cont.)

- Reason for normalizing a relation : *Simplicity!!* 
  - <e.g.> Consider two transactions T1, T2: Transaction T1 : insert ('S5', 'P6', 500)

Transaction T2 : insert ('S4', 'P6', 500)

There are difference:

- Un-normalized: two operations (one insert, one append)
- Normalized: <u>one</u> operation (insert)

# **Kinds of Relations**

- **Base Relations (Real Relations):** a named, atomic relation; a direct part of the database. e.g. S, P
- Views (Virtual Relations): a named, derived relation; purely represented by its definition in terms of other named relations.
- Snapshots: a named, derived relation with its own stored data.
  - <e.g.>

٠

CREATE SNAPSHOT SC		
AS SELECT S#, CITY	Relation	London Supplier
FROM S	Ļ	View
REFRESH EVERY DAY;	OP	
A read-only relation.	Ļ	
Periodically refreshed	Relation	
renouloung renobiled		Base table Base table

- **Query Results:** may or may not be named, no persistent existence within the database.
- Intermediate Results: result of subquery, typically unnamed.
- **Temporary Relations:** a named relation, automatically destroyed at some appropriate time.

# **Relational Databases**

- Definition: A Relational Database is a database that is perceived by the users as a collection of <u>time-varying</u>, <u>normalized</u> relations.
  - *Perceived by the users:* the relational model apply at the <u>external</u> and <u>conceptual</u> levels.
  - *Time-varying:* the set of tuples changes with time.
  - *Normalized:* contains no repeating group (only contains atomic value).
- The **relational model** represents a database system at a <u>level of abstraction</u> that removed from the details of the underlying machine, like **high-level language.**



# **3.3 Relational Integrity Rules**

#### **Purpose:**

to inform the DBMS of certain constraints in the real world.

- Candidate keys: Let R be a relation with attributes A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>n</sub>. The set of attributes K (A<sub>i</sub>, A<sub>j</sub>, ..., A<sub>m</sub>) of R is said to be a candidate key iff it satisfies:
  - *Uniqueness:* At any time, no two tuples of R have the same value for K.
  - <u>*Minimum*</u>: none of  $A_i, A_j, ..., A_k$  can be discarded from K without destroying the uniqueness property.

<e.g.> S# in S is a candidate key.

(S#, P#) in SP is a candidate key.

(S#, CITY) in S is not a candidate key.

- **Primary key**: one of the candidate keys.
- Alternate keys: candidate keys which are not the primary key.
  - <e.g.> S#, SNAME: both are candidate keys S#: primary key SNAME: alternate key.
- **Note:** Every relation has at least one candidate key.

S‡	SNAME	STATUS	CITY
S1	Smith	20	London
S	Clark	20	London

# Foreign keys (p.261 of C. J. Date)

- *Foreign keys*: Attribute FK (possibly composite) of base relation R2 is a foreign keys iff it satisfies:
  - 1. There exists a base relation R1 with a candidate key CK, and
  - 2. For all time, each value of FK is identical to the value of CK in some tuple in the current value of R1.



# **Two Integrity Rules of Relational Model**

#### Rule 1: Entity Integrity Rule

No component of the primary key of a base relation is allowed to accept nulls.

#### Rule 2: Referential Integrity Rule

The database must not contain any <u>unmatched foreign</u> key values.

**Note:** Additional rules which is specific to the database can be given. <e.g.> QTY = { 0~1000}

However, they are outside the scope of the relational model.

# **Referential Integrity Rule**

How to avoid against the referential Integrity Rule?

 <u>Delete rule</u>: what should happen on an attempt to delete/update target of a foreign key reference

- RESTRICTED
- CASCADES
- NULLIFIES

<e.g.> User issues:

**DELETE FROM S WHERE S#='S1'** 

System performs:

Restricted:

Reject!

Cascades:

DELETE FROM **SP** WHERE S#='S1'

Nullifies:

UPDATE **SP** SET S#=Null WHERE S#='S1'



# **Foreign Key Statement**

Descriptive statements:

FOREIGN KEY (foreign key) REFERENCES target NULLS [NOT] ALLOWED DELETE OF target <u>effect</u> UPDATE OF target-primary-key <u>effect</u>;

effect: one of {RESTRICTED, CASCADES, NULLIFIES}

<e.g.1> (p.269)

CREATE TABLE **SP** (S# S# NOT NULL, P# P# NOT NULL, QTY QTY NOT NULL, PRIMARY KEY (S#, P#), FOREIGN KEY (S#) REFERENCE S ON DELETE CASCADE ON UPDATE CASCADE, FOREIGN KEY (P#) REFERENCE P ON DELETE CASCADE ON UPDATE CASCADE, CHECK (QTY>0 AND QTY<5001));

# **3.4 Relational Algebra**

# **Introduction to Relational Algebra**

- The relational algebra consists of a collection of <u>eight high-level operators</u> that **operate on relations**.
- Each operator takes relations (one or two) as operands and produce a relation as result.
  - the important property of closure.
  - nested relational expression is possible.

## Introduction to Relational Algebra (cont.)

- Relational operators: [defined by Codd, 1970]
  - Traditional set operations:
    - Union  $(\cup)$
    - Intersection  $(\cap)$
    - Difference (–)
    - Cartesian Product / Times (x)
  - Special relational operations:
    - Restrict ( $\sigma$ ) or Selection
    - Project  $(\Pi)$
    - Join (⋈)
    - Divide (÷)

## **Relational Operators**



### **Relational Operators** (cont.)



# **SQL vs. Relational Operators**

#### • A SQL SELECT contains several relational operators.



#### BNF (p. 3-44)

# **Traditional Set Operations**

• Union Compatibility: two relations are union compatible iff they have <u>identical headings</u>.

i.e.:

- 1. they have same set of attribute name.
- 2. corresponding attributes are defined on the same domain.
- objective: ensure the result is still a relation.
- Union (∪), Intersection (∩) and Difference (−) require Union Compatibility, while Cartesian Product (X) don't.

# **Traditional Set Operations: UNION**

- **A**, **B**: two <u>union-compatible</u> relations.
  - $A: (X_1, ..., X_m)$
  - $B : (X_1, ..., X_m)$
  - A UNION B:
    - Heading:  $(X_1,...,X_m)$
    - **Body:** the set of all tuples t belonging to either A or B (or both).
  - Association:

 $(A \cup B \ ) \cup C = A \cup (\ B \cup C)$ 

• Commutative:

$$A \cup B = B \cup A$$



### **Traditional Set Operations: INTERSECTION**

• A, B: two <u>union-compatible</u> relations.

 $A: (X_1, ..., X_m)$ 

- $B : (X_1, ..., X_m)$
- A INTERSECT B:
  - Heading:  $(X_1,...,X_m)$
  - **Body:** the set of all tuples t belonging to **both** A and B.
- Association:

 $(A \cap B) \cap C = A \cap (B \cap C)$ 

• Commutative:

$$A \cap B = B \cap A$$



# **Traditional Set Operations: DIFFERENCE**

- **A**, **B**: two <u>union-compatible</u> relations.
  - $A : (X_1, ..., X_m)$
  - $B:(X_1,...,X_m)$
- A MINUS B:
  - Heading:  $(X_1,...,X_m)$
  - **Body:** the set of all tuples t belonging to A and not to B.

Α

• Association: No!

$$(A - B) - C \neq A - (B - C)$$

• Commutative: No!

 $A-B\neq B-A$ 



### **Traditional Set Operations: TIMES**

Extended Cartesian Product (x):

Given:

A = { a | a = 
$$(a_1, ..., a_m)$$
 }

- $B = \{ b \mid b = (b_1, ..., b_n) \}$
- Mathematical Cartesian product:

• Extended Cartesian Product:

A x B = { t | t= 
$$(a_1,...,a_m,b_1,...,b_n)$$
 }  
Coalescing

<u>math.</u>

$$A = \{x, y\}$$
  
B = {y, z}  
A x B = {(x,y),(x,z),(y,y),(y,z)}

• <u>**Product Compatibility:**</u> two relations are product-compatible iff their <u>*headings are*</u> <u>*disjoint.*</u>

### Traditional Set Operations: TIMES (cont.)



S x P (S#, ..., CITY, ..., CITY)

S and P are *not* product compatible!



P RENAME CITY AS PCITY;

S x P (S#, ..., CITY, ..., **PCITY**)

### Traditional Set Operations: TIMES (cont.)

- A, B: two product-compatible relations. A: (X<sub>1</sub>,...,X<sub>m</sub>), A = { a | a = (a<sub>1</sub>,...,a<sub>m</sub>) } B: (Y<sub>1</sub>,...,Y<sub>n</sub>), B = { b | b = (b<sub>1</sub>,...,b<sub>n</sub>) }
  A TIMES B: (A x B)
  Heading: (X<sub>1</sub>,...,X<sub>m</sub>,Y<sub>1</sub>,...,Y<sub>n</sub>)
  - **Body:** {  $c | c = (a_1, ..., a_m, b_1, ..., b_n)$  }
- Association:
  - (A x B) x C = A x (B x C)
- Commutative:

$$A \times B = B \times A$$



AXB

S#

S1

**S**1

P#

P1

P2

# Special Relational Operations: Restriction

- Restriction: a unary operator or monadic
  - Consider: A: a relation, X,Y: attributes or literal
  - **theta-restriction** (or abbreviate to just 'restriction'):

A WHERE X theta Y or  $\mathbf{O}_{X \text{ theta } Y}$  (A) (By Date) ( $\theta$ ) (By Ullman) (By Ullman) (Here) ( $\mathbf{O}_{X \text{ theta } Y}(\mathbf{A})$  (By Ullman) ( $\mathbf{O}_{X \text{ theta } Y}(\mathbf{A})$  ( $\mathbf{O}_{X \text{ th$ 



• The restriction condition (X theta Y) can be extended to be any Boolean combination by including the following equivalences:

 $(1) \sigma_{C1 \text{ and } C2}(A) = \sigma_{C1}(A) \cap \sigma_{C2}(A); \quad (2) \sigma_{C1 \text{ or } C2}(A) = \sigma_{C1}(A) \cup \sigma_{C2}(A); \quad (3) \sigma_{not C}(A) = A - \sigma_{C}(A)$ 

• <e.g.> S WHERE CITY='London'? or  $\sigma_{CITY='London'}(S)$ 



# Special Relational Operations: Projection

- Projection: a unary operator.
  - Consider:

A : a relation X,Y,Z : attributes

- A[X,Y,Z] or  $\prod_{X,Y,Z}(A)$
- Identity projection: A = A or  $\Pi(A) = A$
- Nullity projection: A[] =  $\emptyset$  or  $\prod_{\emptyset}(A) = \emptyset$



# **Special Relational Operations: Natural**

Join

- Natural Join: a binary operator.
  - Consider:
    - A:  $(X_1,...,X_m, Y_1,...,Y_n)$
    - $B: (Y_1, ..., Y_n, Z_1, ..., Z_p)$
  - A JOIN B (or A⋈B): common attributes appear only once. e.g. CITY (X<sub>1</sub>,...,X<sub>m</sub>, Y<sub>1</sub>,...,Y<sub>n</sub>, Z<sub>1</sub>,...,Z<sub>p</sub>);
  - Association:
    - $(A \bowtie B) \bowtie C = A \bowtie (B \bowtie C)$
  - Commutative:
    - $A \bowtie B = B \bowtie A$
  - if A and B have no attribute in common, then
    - $A \bowtie B = A \times B$

### **Special Relational Operations: Natural Join**

#### (cont.)

<e.§< th=""><th>g.&gt;</th><th colspan="7">&gt; <math>\begin{array}{l} S \text{ JOIN } P \\ S.city = P.city \end{array}</math> or <math>\begin{array}{l} S \bowtie P \\ S.city = P.city \end{array}</math></th></e.§<>	g.>	> $\begin{array}{l} S \text{ JOIN } P \\ S.city = P.city \end{array}$ or $\begin{array}{l} S \bowtie P \\ S.city = P.city \end{array}$						
	S		-			Р		
S#	SNAME	STATUS	CITY	P#	PNAME	COLOR	WEIGHT	CITY
S1	Smith	20	London	P1	Nut	Red	12	London
S1	Smith	20	London	P4	Screw	Red	14	
S1	Smith	20	London	P6	Cog	Red	19	
S2	Jones	10	Paris	P2	Bolt	Green	17	
S2	Jones	10	Paris	P5	Cam	Blue	12	
S3	Blake	30	Paris	P2	Bolt	Green	17	
S3	Blake	30	Paris	P5	Cam	Blue	12	
S4	Clark	20	London	P1	Nut	Red	12	
S4	Clark	20	London	P4	Screw	Red	14	
S4	Clark	20	London	P6	Cog	Red	19	

### **Special Relational Operations: Theta Join**

- **A, B:** product-compatible relations, A:  $(X_1,...,X_m)$ , B:  $(Y_1,...,Y_n)$
- theta : =, <>, <, >,.....
- $A \bowtie B_{X \text{ theta } Y} = \mathbf{O}_{X \text{ theta } Y}(A \times B)$
- If theta is '=', the join is called *equijoin*.



 $\sigma_{\text{CITY} > \text{PCITY}}(S \text{ x (P RENAME CITY AS PCITY)})$ 

#### $\checkmark$

S#	SNAME	STATUS	CITY	P#	PNAME	COLOR	WEIGHT	PCITY
S2	Jones	10	Paris	P1	Nut	Red	12	London
S2	Jones	10	Paris	P4	Screw	Red	14	London
S2	Jones	10	Paris	P6	Cog	Red	19	London
S3	Blake	30	Paris	P1	Nut	Red	12	London
S3	Blake	30	Paris	P4	Screw	Red	14	London
S3	Blake	30	Paris	P6	Cog	Red	19	London

## **Special Relational Operations: Division**

- Division:
  - A, B: two relations.
    - A :  $(X_1,...,X_m, Y_1,...,Y_n)$ B :  $(Y_1,...,Y_n)$
  - A DIVIDEBY B (or A ÷ B):
    - Heading:  $(X_1,...,X_m)$
    - **Body:** all (X:x) s.t. (X:x,Y:y) in A for all (Y:y) in B

<e.g.> "Get supplier numbers for suppliers who supply all parts."



# Special Relational Operations: primitive

- Which of the eight relational operators are <u>primitive</u>?
  - 1. UNION
  - 2. DIFFERENCE
  - **3. CARTESIAN PRODUCT**
  - 4. RESTRICT
  - 5. PROJECT
- How to define the non-primitive operators by those primitive operators?



 $\Pi_{S\#,SNAME,STATUS,CITY,P\#,PNAME,COLOR,WEIGHT} (\sigma_{CITY=PCITY} (S X (P RENAME CITY AS PCITY)))$ 

# Special Relational Operations: primitive (cont.)

 $\bigcirc$  INTERSECT: A  $\cap$  B = A – (A – B)



# Special Relational Operations: primitive (cont.)

**③**DIVIDE:  $A \div B = A[X] - (A[X] \times B - A)[X]$ 



# **BNF Grammars for Relational Operator**

- 1. expression ::= monadic-expression | dyadic-expression
- 2. monadic-expression ::= renaming | restriction | projection
- 3. renaming ::= term RENAME attribute AS attribute
- 4. term ::= relation | (expression )
- 5. restriction ::= term WHERE condition
- 6. Projection ::= attribute | term [attribute-commalist]
- 7. dyadic-expression ::= projection dyadic-operation expression
- 8. dyadic-operation ::= UNION | INTERSECT | MINUS | TIMES | JOIN | DIVIDEBY



(Back to p. 3-27)

# **BNF Grammars for Relational Operator**



# Relational Algebra v.s. Database Language:

Example : Get supplier name for suppliers who supply part P2.
 SQL:
 SWAME STATUS CITY S#

SELECT S.SNAME FROM S, SP WHERE S.S# = SP.S# AND SP.P# = 'P2'

S#	SNAME	STATUS	CIT Y	S#	P#	QTY
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P1	300
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P2	200
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P3	400
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P4	200
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P5	100
<b>S</b> 1	Smith	20	London	<b>S</b> 1	P6	100
<b>S</b> 2	Jones	10	Paris	<b>S</b> 2	P1	300
<b>S</b> 2	Jones	10	Paris	<b>S</b> 2	P2	400
<b>S</b> 3	Blake	30	Paris	<b>S</b> 3	P2	200
<b>S</b> 4	Clark	20	London	<b>S</b> 4	P2	200
<b>S</b> 4	Clark	20	London	<b>S</b> 4	P4	300
<b>S</b> 4	Clark	20	London	<b>S</b> 4	P5	400

#### • Relational algebra:

(( S JOIN SP) WHERE P# = 'P2') [SNAME]

or

$$\Pi_{\text{SNAME}} \left( \sigma_{\text{P}\#='\text{P2}'} \left( S \bowtie S P \right) \right)$$

# What is the Algebra for?

- (1) Allow writing of expressions which serve as a high-level (SQL) and symbolic representation of the users intend.
- (2) Symbolic transformation rules are possible.

A convenient basis for <u>optimization</u>!

e.g. (( S JOIN SP ) WHERE P#='P2')[SNAME] = (S JOIN ( SP WHERE P#='P2')) [SNAME] (p.544; p.11-12)

Back to p.3-66

# **3.5 Relational Calculus**

### **Introduction to Relational Calculus**

- A notation for expressing the definition of some new relations in terms of some given relations.
  - < e.g. > SP.P#, S.CITY WHERE SP.S# = S.S# definition predicate
- Based on first order predicate calculus (a branch of mathematical logic).
  - Originated by Kuhn for database language (1967).
  - Proposed by Codd for relational database (1972)
  - ALPHA: a language based on calculus, never be implemented.
  - QUEL: query language of INGRES, influenced by ALPHA.
- Two forms :
  - Tuple calculus: by Codd..
  - Domain calculus: by Lacroix and Pirotte.



# **Tuple Calculus**

#### BNF Grammar:

<e.g.> "Get supplier number for suppliers in Paris with status > 20"

#### **Tuple calculus expression:**



### Tuple Calculus (cont.)



Tuple variable (or Range variable):

• A variable that "range over" some named relation.

<e.g.>:

In QUEL: (Ingres)

- RANGE OF SX IS S;
- RETRIEVE (SX.S#) WHERE SX.CITY = "London"



## Tuple Calculus (cont.)

• Implicit tuple variable:

<e.g.> <u>In SQL:</u> <u>SELECT S.S# FROM S WHERE S.CITY = 'London'</u> <u>In QUEL:</u> <u>RETRIEVE (SX.S#) WHERE SX.CITY='London'</u>

# **Tuple Calculus: BNF**

1. range-definition

::= RANGE OF variable IS range-item-commalist

2. range-item

- ::= relation | expression
- 3. expression

::= (target-item-commalist) [WHERE wff]

4. target-item

::= variable | variable . attribute [ AS attribute ]

#### 5. wff

::= condition | NOT wff | condition AND wff | condition OR wff | IF condition THEN wff | EXISTS variable (wff) | FORALL variable (wff) | (wff)

# Tuple Calculus: BNF - Well-Formed Formula

#### (WFF)

- (a) Simple comparisons:
  - SX.S# = 'S1'
  - SX.S# = SPX.S#
  - SPX.P# <> PX.P#
- (b) Boolean WFFs:
  - NOT SX.CITY='London'
  - SX.S#=SPX.S# AND SPX.P#<>PX.P#
- (c) Quantified WFFs:
  - EXISTS: existential quantifier

<e.g.>

EXISTS SPX (SPX.S#=SX.S# and SPX.P#= 'P2' )

i.e. There exists an SP tuple with S# value equals to the value of SX.S# and P# value equals to 'P2'

• FORALL: universal quantifier

<e.g.>

FORALL PX(PX.COLOR = 'Red') i.e. For all P tuples, the color is red.

<Note>: FORALL x(f) = NOT EXISTS X (NOT f)



[Example 1]: Get Supplier numbers for suppliers in Paris with status > 20

- SQL: SELECT S# FROM S WHERE CITY = 'Paris' AND STATUS >20
- Tuple calculus:

SX.S# WHERE SX.CITY= 'Paris' AND SX.STATUS > 20

• Algebra:

 $\Pi_{S^{\#}}\left(\boldsymbol{\boldsymbol{\mathsf{\sigma}}}_{\mathrm{CITY='Paris', and STATUS>20}}(S)\right)$ 

[Example 2]: Get all pairs of supplier numbers such that the two suppliers are located in the same city.

Rename S FIRST, SECOND

- SQL: (S.S#) (S.S#) SELECT FIRST.S#, SECOND.S# FROM S FIRST, S SECOND WHERE FIRST.CITY = SECOND.CITY AND FIRST.S# < SECOND.S#;
- Tuple calculus:

FIRSTS#=SX.S#, SECONDS# =SY.S# WHERE SX.CITY=SY.CITY AND SX.S# < SY.S#

• Algebra:

 $\Pi_{\text{FIRSTS#,SECONDS#}} (\sigma_{\text{FIRSTS#<SECONDS#}}$ 

 $((\prod_{\text{FIRSTS#,CITY}} (\text{S RENAME S# AS FIRSTS#})) \underset{\text{city=city}}{\bowtie}$ 

 $(\Pi_{\text{SECONDS\#,CITY}}(\text{S RENAME S# AS SECONDS#}))))$ 

{S1, S1} {S1, S4} {S4, S1} {S4, S4} {S4, S4}

{**S1,S4**}{**S2,S3**}

[Example 3]: Get supplier names for suppliers who supply all parts.



[Example 4]: Get part numbers for parts that either weigh more than 16 pounds or are supplied by supplier S2, or both.

• SQL:

SELECT P# FROM P WHERE WEIGHT > 16 UNION SELECT P# FROM SP WHERE S# = 'S2'

• Tuple calculus:

RANGE OF PU IS (PX.P# WHERE PX.WEIGHT>16), (SPX.P# WHERE SPX.S#='S2'); PU.P#;

• Algebra:

 $(\Pi_{\mathtt{P\#}}\left(\boldsymbol{\boldsymbol{\mathsf{O}}}_{\mathtt{WEIGHT}>16}\,\mathtt{P}\right))\cup\left(\Pi_{\mathtt{P\#}}(\boldsymbol{\boldsymbol{\mathsf{O}}}_{\mathtt{S\#='S2'}}\,\mathtt{SP})\right)$ 

[參考用]

### **Relational Calculus v.s. Relational Algebra.**

Algebra	Calculus
Provides explicit operations	Only provide a notation for <i>formulate</i>
[e.g.JOIN, UNION, PROJECT,]	the definition of that desired relation in
to <i>build</i> desired relation from the given relations.	terms of those given relation.
<ul> <li>1&gt; JOIN S with SP on S#</li> <li>2&gt; RESTRICT the result with P# = 'P2'</li> <li>3&gt; PROJECT the result on S# and CITY</li> </ul>	SX.S#, SX.CITY WHERE EXISTS SPX ( SPX.S#=SX.S# AND SPX.P#= 'P2')
Prescriptive (how?)	descriptive (what ?)
Procedural	non-procedural

#### ("expressive power") **Relational Calculus = Relational Algebra**

- Codd's reduction algorithm:
  - 1. Show that any calculus expression can be reduced to an algebraic equivalent.

Algebra ⊇ Calculus

2. show that any algebraic expression can be reduced to a calculus equivalent



$$\checkmark$$

Algebra  $\equiv$  Calculus

# **Relationally Complete**

 Def : A language is said to be *relationally complete* if it is <u>at least as</u> powerful as the relational calculus.

i.e. if any relation definable via a *single expression* of the calculus is definable via a single expression of the language.

<e.g.> SQL,QUEL



• Show a language L is relationally complete

Show that L includes analogs of the <u>five primitive</u> algebraic operation.

Easier than show L is at least as powerful as relational calculus.

#### **Domain Calculus** (Domain-Oriented Relational Calculus)

- Distinctions between <u>domain calculus</u> and <u>tuple calculus</u>:
  - Variables range over *domain* instead of relation.
  - Support an additional form of comparison:
     *the membership condition*

<e.g.1> SP(S#:'S1', P#:'P1')
True iff exists a tuple in SP with S#='S1' and P# = 'P1'
<e.g.2> SP(S#: SX, P#:PX)
True iff exists a tuple in SP with
S#=current value of domain var. SX.
P#=current value of domain var. PX.

Var. SX PX





### **Domain Calculus:** attributes WHERE membership\_condition

Domain Calculus expressions:

e.g.1 SX

e.g. {S1, ..., (i.e. all possible values of supplier number) **S**100} e.g.2 SX WHERE S(S#:SX) e.g. {S1, ...,

(i.e. all S# in relation S)

**S**4}

#### e.g.3 SX WHERE S(S#:SX, CITY:'London')

(i.e. subset of S# in S for which city is 'London')



(i.e. subset of S# and CITY in S for the suppliers who supply P2)

#### **Tuple Calculus:** term WHERE wff

**Domain Calculus:** term WHERE m-c

# Query-by-Example (QBE)

- An attractive realization of the <u>domain calculus</u>
- Simple in syntax
- e.g. Get supplier numbers for suppliers in Paris with status > 20

#### • Tuple calculus:

SX.S# WHERE SX.CITY= 'Paris' AND SX.STATUS > 20

• Domain calculus:

SX

WHERE EXISTS STATUSX

(STATUSX >20) AND

S(S#:SX, STATUS:STATUSX, CITY:'Paris')

• QBE:

S	S#	SNAME	STATUS	CITY	<b>– – –</b> <i>– – – – – – – – – –</i>
	P.		>20	"Paris"	P. : print or present

# Query-by-Example (cont.)

[Example]: Get all pairs of supplier numbers such that the two suppliers are located in the same city.

• SQL: SELECT FIRST.S#, SECOND.S#

FROM S FIRST, S SECOND

WHERE FIRST.CITY = SECOND.CITY AND FIRST.S# < SECOND.S#;

• Tuple calculus:

FIRSTS# = SX.S#, SECONDS# = SY.S#

WHERE SX.CITY = SY.CITY AND SX.S# < SY.S#

• Domain calculus:

$$S_1, S_4$$
 FIRSTS# = SX, SECONDS# = SY

{S<sub>2</sub>, S<sub>3</sub>} WHERE EXISTS CITYZ

(S(S#:SX,CITY:CITYZ) AND S(S#.SY,CITY:CITYZ) AND SX<SY)

• QBE:





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# **Concluding Remarks**

Relational <u>algebra</u> provide a convenient target language as a vehicle for a possible implementation of the <u>calculus</u>.

Query in a calculus-based language. e.g. SQL, QUEL, QBE, ... Codd reduction algorithm Equivalent algebraic expression Optimization (p. 3-47)more in Unit 11 More efficient algebraic expression Evaluated by the already implemented algebraic operations
Unit 11 e.g. Join

#### Result

# Concluding Remarks (cont.)

A spectrum of data management system:

- S: Structure (Table)
- M: Manipulative
- I: Integrity



# **Foreign Key Statement**

#### Descriptive statements:

FOREIGN KEY (foreign key) REFERENCES target NULLS [NOT] ALLOWED DELETE OF target <u>effect</u> UPDATE OF target-primary-key <u>effect</u>;

effect: one of {RESTRICTED, CASCADES, NULLIFIES}

<e.g.1> (p.269)

CREATE TABLE **SP** (S# S# NOT NULL, P# P# NOT NULL, QTY QTY NOT NULL, PRIMARY KEY (S#, P#), FOREIGN KEY (S#) REFERENCE S ON DELETE CASCADE ON UPDATE CASCADE, FOREIGN KEY (P#) REFERENCE P ON DELETE CASCADE ON UPDATE CASCADE, CHECK (QTY>0 AND QTY<5001));



# **SQL vs. Relational Operators**





#### BNF (p. 3-44)